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TenCate Advance Composites IM7 GP Unitape with BT250E-6 Resin Material Allowables Statistical Analysis Report

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1.

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1.1 Symbols and Abbreviations

Table 1-1: Test Property Abbreviations

Transverse Compression Poisson's Ratio $_{21}^{\circ}$

1.2 Pooling Across Environments

When pooling across environments was allowable, pooled co-efficient of ariation was used. CMH17 STATS v2011 r1.1 was used to determing origing was allowable and to compute the pooled coefficient of variation for those tests. In these cases, ritualified coefficient of variation based on the pooled data was used to compute the basis values.

When pooling across environments was not advesto because the data was not eligible for pooling and engineering judgment indicated there no justification for overriding the result, then B-Basis values were computed for each environmental condition separately, which are also provided by CMH17 STATS.

1.3 Basis Value Computational Process

The general form to computengineering basis values is asis value \bar{x} kS where k is a factor based on the sample sized the distribution of the sampliata. There are many different methods to determine the value lofin this equation, depending on the sample size and the distribution of the data. In addition, the comptidinal formula used for the standard deviation, S, may vary depending on the distribution of the datal details of those different computations and when each should beed are in section 2.0.

1.4 Modified Coefficient of Variation (CV) Method

A common problem with new matel qualifications is that the initial specimens produced and tested do not contain all of the variability that be encountered when the material is being produced in larger amounts over a lengthy periotine. This can result in setting basis values that are unrealistically high. The ariability as measured in chequalification program is often lower than the actual material variability because everal reasons. The aterials used in the qualification programs are usually analytic within a short peak of time, typically $2-3$ weeks only, which is not represet ive of the production material ome raw ingredients that are used to manufacture the multi-batch qualification materials may actually be from the same production batches or maliauxtured within a short period dime so the qualification materials, although regarded as multiple batches, may truck be multiple batches so they are not representative of the actuaboluction material variability.

The modified Coefficient of Variation (CV) used this report is in accordance with section 8.4.4 of CMH-17-1G. It is a method of adjunsti the original basis values downward in anticipation of the expected additial variation. Composite matal is are expected to have a CV of at least 6%. The modified coefficient **vanilation** (CV) method increases the measured coefficient of variation when it is below 8% pre qualification prog18i for to comwild

The material allowables in this report are alculated using both the as-measured CV and modified CV, so users have the boice of using either one. When the measured CV is greater than 8%, the modified CV method does notarchie the basis value. NCAMP recommended values make use of the modified CV hor when it is appropriate for the data.

When the data fails the Anderson-Darling K-saminest for batch to batch variability or when the data fails the normality test, the modified $\mathbf{\Omega}$ ethod is not approptic and no modified CV basis value will be provided. When the ANOVA ethod is used, it may produce excessively conservative basis values. When appropriate ingle batch or two batch estimate may be provided in addition to the ANOVA estimate.

In some cases a transformation of the data to assumption of the modified CV resulted in the transformed data passing the ADK test and the stata can be pooled only for the modified CV method.

NCAMP recommends that if a user decides to the basis values that are calculated from asmeasured CV, the specification limits and controlt time calculated with as-measured CV also. Similarly, if a user decides to use the basibles that are calculated from modified CV , the specification limits and control limits be calculated that modified CV also. This will ensure that the link between material allowables, spection limits, and control limits is maintained.

2. Background

Statistical computations are performed with GMW STATS. Pooling across environments will be used whenever it is permissible accound to CMH-17-1G guidelines. If pooling is not permissible, the results of single point analysis provideby CMH17 STATS is included instead. If the data does not meantle-17-1G requirements for angile point analysis, estimates are created by a variety of theds depending on which is mosp propriate for the dataset available. Specific procedures used are predeinte individual sections where the data is presented.

2.1 CMH17 STATS Statistical Formulas and Computations

This section contains the details of the pecific formulas CMH17 STATS uses in its computations.

2.1.1

Wherek refers to the number of batch**e**sindicates the stadard deviation ofth sample, and it refers to the number of specimens in ithe ample.

2.1.2.2 Pooled Coefficient of Variation

Since the mean for the normalized data is 1.0 for each condition, the pooled normalized data also has a mean of one. The coefficient of variatior the pooled normalized data is the pooled standard deviation divided by the oled mean, as in equation 3. Since the mean for the pooled i

Step 1: Apply the modified CV rules teach batch and compute the modified standard deviation

If MNR $>$ C, then the X_i associated with the MNR is consider tead be an outlier. If an outlier exists, then the associated with the MNR is dropped for the dataset and the MNR procedure is applied again. This process is repeated no outliers are detected. Additional information on this procedure can be found in references 1 and 2.

2.1.6 The k-Sample Anderson Darling Test for Batch Equivalency

The k-sample Anderson-Darling test is a nonpertatic statistical procedure that tests the hypothesis that the populations from tich two or more groups of the were drawn are identical. The distinct values in the combined data ane ordered from smallest to largest, denoted $z_{(2)}, \ldots, z_{L}$, where L will be less than n if there are tied observations. These rankings are used to compute the test statistic.

The k-sample Anderson-Darg test statistic is:

$$
\begin{array}{llll}\n\text{ADK} & \frac{n}{n^2(k-1)} \int_{i=1}^{k} \frac{1}{n} \int_{j=1}^{L} h_j \frac{n F_{ij} - n H_j \frac{1}{\alpha}}{H_j - n H_j \frac{n h_j \alpha}{4 \alpha}} & \text{Equation 25}\n\end{array}
$$

Where

 $n =$ the number of test specimens in each batch

 $n = n_1 + n_2 + ... + n_k$

 h_j = the number of values in the combined samples equal to H_i

```
b (2g \ 4)k^2 8Tk (2g \ 14T \ 4)S 8T 4g \ 6c (6T 2g 2)k^2 (4T 4g 6)k (2T 6)S 4T
d (2T 6)k^2 4Tk
    1
   <sup>n</sup> 1<sub>1</sub>
   <sub>i 1</sub> i
   n 2 n 1 1
g \frac{1}{i+j+1}a (4g 6)(k 1) (10 6g)S
    1
k
   i 1 <sup>I i</sup>i
S
    n_1T
```
An observed significance level (OSL) based on Amderson-Darling test statistic is computed for each test. The OSL measures the probability bserving an Anderson-Darling test statistic at least as extreme as the value calculated if distribution under consideration is in fact the underlying distribution of the da. In other words, the OSL is the probability of obtaining a value of the test statistiat least as large abat obtained if the hypothsis that the data are actually from the distribution being tested is true. If the OSL is less than or equal to 0.05, then This approximation is accurate to within 0.2% the tabulated values for sample sizes greater than or equal to 16.

2.2.2.2 One-sided A-basis tolerance factors, A , for the normal distribution

The exact computation of values is \sqrt{n} times the 0.95th quantile of the noncentral t-distribution with noncentrality paramet α 326 n and n i 1 degrees of freedom (Reference 11). Since this is not a calction that Excel can handle easity following approximation to the k_B values is used:

2.2.2.3.2 Goodness-of-fit test forthe Weibull distribution

The two-parameter Weibull distribution is contated by comparing the cumulative Weibull distribution function thabest fits the data with the cumulativ distribution function of the data.

$$
V_A \quad 6.649 \quad exp \quad 2.55 \quad 0.526 \text{ Im} \left(\begin{array}{cc} 4.76^{\circ} \\ \frac{\alpha}{2} \end{array} \right) \qquad \qquad \text{Equation 46}
$$

Equation 46

This approximation is accurate within 0.5% of the tabulated values of example requal to 16.

Weibull Dist. K Factors for N<16		
Ν	B-basis	A-basis
2	690.804	1284.895
3	47.318	88.011
4	19.836	36.895
5	13.145	24.45
6	10.392	19.329
$\overline{7}$	8.937	16.623
8	8.047	14.967
9	7.449	13.855
10	6.711	12.573
11	6.477	12.093
12	6.286	11.701
13	6.127	11.375
14	5.992	11.098
15	5.875	10.861

Table 2-2: Weibull Distribution Basis Value Factors

2.2.2.4 Lognormal Distribution

A probability distribution for whib the probability that an obsertion selected at random from this population falls between and $\mathfrak b$ o a $\mathfrak b$ is given by the area under the normal distribution betweeln(a) and $ln(b)$.

The lognormal distribution is a posity skewed distributio that is simply related to the normal distribution. If something is a prormally distributed, then its garithm is normally distributed. The natural (base e) logarithm is used.

2.2.2.4.1 Goodness-of-fit test for the Lognormal distribution

In order to test the goodness-difect the lognormal distribution, kee the logarithm of the data and perform the Anderson-Darling test for normality from Section 2.1.7. Using the natural logarithm, replace the linked equatiabove with linked equation below:

$$
z_i = \frac{\ln x_i - \overline{x}_i}{s_i}, \quad \text{for } i \neq 1, \dots, n
$$

Equation 47

where x_i is the th smallest sample observatiox, and **s** are the mean and standard deviation of the $ln(x)$ values.

The Anderson-Darling statistic is then computiting the linked equation above and the observed significance level (OSIs computed using the linke equation above. This OSL measures the probability of observing an Ander Barling statistic at least as extreme as the

value calculated if in fact the data are ample from a lognormal distribution. If OSLI0.05, one may conclude (at a five percent risk of bein error) that the population is not lognormally distributed. Otherwise, the hyposis that the population is gnormally distributed is not rejected. For further information on these procedures, see reference

2.2.2.4.2 Basis value calculations fothe Lognormal distribution

If the data set is assumed to be from a population a lognormal distribution, basis values are calculated using the equation above in section 32. However, the calculations are performed using the logarithmef the data rather than the original observations. The computed basis values are then transformed back to the original unitsropplying the inverse of

2.2.3.2 Non-parametric Basis Values for small samples

The Hanson-Koopmans method (references 8 and 0\$ed for obtaining a B-basis value for sample sizes not exceeding 28 and A-basis values fople sizes less than 299. This procedure requires the assumption that the observations andom sample from a population for which

2.2.4.1 Calculation of basis values using ANOVA

The following calculations addresstolato-batch variability. In the words, the only grouping is due to batches and the k-sample Anderson-**Datest** (Section 2.1.6) indicates that the batch to batch variability is too large to pool the data. The method is based on the one-way analysis of variance random-effects model, and the produce is documented in reference 10.

ANOVA separates the total variation (called thensof squares) of the data into two sources: between batch variation and thin batch variation.

First, statistics are computed for each cha which are indicated with a subscript, \bar{x} , \hat{s}

while statistics that were computed with the resultataset do not have subscript. Individual data values are represed with a double subscripthe first number indiated the batch and the second distinguishing between the indivaduata values within the batch is stands for the number of batches in the analysis. With thetatistics, the Sum of Squares Between batches (SSB) and the Total Sum of Squares (SST) are computed:

> 2×2 1 k i I i SSB ¦ ก⊀ี กิxิ $\frac{1}{1}$ \overrightarrow{n} \overrightarrow{x} \overrightarrow{n} \overrightarrow{x} \overrightarrow{n} Equation 52 $\frac{2}{5}$ 1 1 k ni ij i j $SST \begin{array}{cc} | & | & \hat{\chi} & \bar{n}\hat{\chi} \end{array}$ $\begin{array}{ccc} | & | & \hat{\mathbf{x}} & \overrightarrow{n}\hat{\mathbf{x}} \\ | & | & | & \hat{\mathbf{x}} & \overrightarrow{n}\hat{\mathbf{x}} \end{array}$ Equation 53

The within-batch, or error, sum of squares (SSE) is computed by subtraction

$$
SSE = SST \quad \text{(SSB)} \tag{Equation 54}
$$

Next, the mean sums of squares are computed:

MSB	$\frac{SSB}{k}$	Equation 55
MSE	$\frac{SSE}{n k}$	Equation 56

Since the batches need not have equal numbers perfacionens, an 'effective batch size,' is defined as

n c
$$
\frac{n}{\frac{1}{n} \prod_{i=1}^{k} n_i^2}{n}
$$
 Equation 57

Using the two mean squares and the effective baize, an estimate dife population standard deviation is computed:

S
$$
\sqrt{\frac{\text{MSB}}{\text{n}}} = \frac{\text{nc 1}\$}{\text{n} \text{c}}
$$

 $\frac{1}{\text{n} \text{c}}$
 $\frac{1}{\text{n} \text{c}}$
 Equation 58

Two k-factors ap0 computed using the methodologyTf 4section 2.2.2 using a sample sizeof 4 n

However, if the laminate CV is larger thare to bresponding lamina CV, the larger laminate CV value is used.

The LVM B-basis value is then computed as:

LVM Estimated B-Basis = \overline{X}_1 K $_{N_1,N_2}$ \overline{X}_1 max CV_1, CV_2 \overline{C} Equation 62

When used in conjunction with the modified CV

3. Summary of Results

The basis values for all tests are summarized tollowing tables. The NCAMP recommended B-basis values meet all requirements of CMH1₃- However, not all test data meets those requirements. The summary tables wide a complete listing of all computed basis values and estimates of basis values. Data that does meet the requirements of CMH-17-1G are shown in shaded boxes and labeled as estimates. Basis vading atted with the modified coefficient of variation (CV) are presented whenever possi**Ble** is values and estimates computed without that modification are presented for all tests.

3.1 NCAMP Recommended B-basis Values

The following rules are used in determining what the value, if any, is not uded in Table 3-1 of the recommended values.

- 1. Recommended values are NEVER estima@ aly B-basis values that meet all requirements of CMH-17-1G are recommended.
- 2. Modified CV basis values are preferred the commended values will be the modified CV basis value when available. The **C**M bovided with the recommended basis value will be the one used in the computation of the basis value.
- 3. Only normalized basis values are given properties that are normalized.
- 4. ANOVA B-basis values are note commended since only three tches of material are available and CMH-17-1G recomm

Lamina Strength Tests

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3.2 Lamina Summary Tables

Values shown in shaded boxes do not meet CMH17 Rev G requirements and are estimates only

4. Test Results, Statistics, Basis Values, and Graphs

Test data for fiber dominated properties was normalized according to nominal cured ply thickness. Both normalized and as-measured titativere included in the tables, but only the normalized data values were graphed. Testures, outliers and explanations regarding computational choices were noted hime accompanying text for each test.

All individual specimen resultare graphed for each test botch and environmental condition with a line indicating the recomended basis values for each is enmental condition. The data is jittered (moved slightly to the left or right) order for all specimen values to be clearly visible. The strength values and ways graphed on the vertical is with the scale adjusted to include all data values and theorresponding basis values. The rical axis may not include

4.1 Longitudinal Tension (LT)

The longitudinal tension stngths are normalized. Pooling across the environments was acceptable with the exception of the normalized Colataset. That dataset failed the Anderson Darling k-sample test (ADK test)

4.2

Table 4-3: Statistics and Basis Values for TT Strength data as-measured

Env CTD RTD ETW

4.4 Transverse Compression (TC)

Transverse Compression datanist normalized for unidirect hall tape. The RTD and ETW datasets failed the Anderson Darling k-sampte (ADK test) for bat to batch variability, which means that pooling across environments not acceptable and MH-17-1G quidelines required using the ANOVA analysis. With fewer thabal 5 chassies, this is consided an estimate.

When the ETW dataset was transformed accord the assumptions of the modified CV method, it passed the ADK test, so the modified as values are provided. The dataset for the RTD condition failed the ADK test after the diffied CV transform, so only estimates are provided for that condition. No nodified CV basis values aprovided for the CTD condition due to the CV being above 8%.

4.5 In-Plane Shear (IPS)

In Plane Shear data is not normalized. The streatch S% strain datasets for the CTD and RTD conditions failed the Anderson Darling k-samplet (ADK test) for batch batch variability, which means that pooling across environments not acceptable and MH-17-1G quidelines required using the ANOVA analysis. With fewer thabal 5 chassies, this is consided an estimate.

When these datasets were transformed accorditing to assumptions of the modified CV method, both passed the ADK test, so the modified basis values are provided.

There were two outliers, both in the CTD conditi The largest value in batch three of the strength at 5% strain dataset and the largesevalbatch two of the 0.2% offset strength dataset

4.6 "33/0/67" Unnotched Compression 0 (UNC0)

The UNC0 data is normalized. The CTD datas weth normalized and as-measured, and the normalized ETW dataset all failed the Andersoming k-sample test (DK test) for batch to batch variability, which meant that pooling as environments was not acceptable and CMH-17-1G guidelines required usit to ANOVA analysis. With fewet than 5 batches, this is considered an estimate.

When the normalized ETW dataset was transformed according to the assumptions of the modified CV method, it passed the ADK test, so the modified CV basis values are provided. The datasets for the CTD condition failed the ADK tater the modified CV transform, so only estimates are provided for that condition.

There were no outliers.

Statistics and estimates of basis values arengior strength data in Table 4-11 and for the modulus data in Table 4-12. The normalized data the B-estimates are shown graphically in Figure 4-6.

4.7 Lamina Short-Beam Strength (SBS)

The Short Beam Strength data is not normalized. SBS datasets failed the Anderson Darling k-sample test (ADK test) for batch to batch riability, which mean that pooling across environments was not acceptable and CMT+14G guidelines required using the ANOVA analysis. With fewer than 5 batches, this is c

Table 4-13: Statistics and Basis Values for SBS data

5. Outliers

Outliers were identified according to the standadd cumented in section 2.1.5, which are in accordance with the guidelines developed in section 8.3.3 of CMH-17-1G. An outlier may be an outlier in the normalized data, the as-measured dat both. A specimen may be an outlier for the batch only (before pooling the three batching a condition together or for the condition (after pooling the three batches within condition together) or both.

Approximately 5 out of 100 specimens will be idened as outliers due to the expected random variation of the data. This testused only to identify specimens to be investigated for a cause of the extreme observation. Outliers that have **antidable** cause are removed from the dataset as they inject bias into the computation of statistiand basis values. Specimens that are outliers for the condition and in both the moalized and as-measured data typically more extreme and more likely to have a specific cause and benoveed from the dataset than other outliers. Specimens that are outliers only for the batount not the condition and specimens that are identified as outliers only for the normalized data or the as-measured data but not both, are typical of normal random variation.

All outliers identified were investigated to telemine if a cause coulde found. Outliers with causes were removed from the taste and the remaining specimens were analyzed for this report. Information about specimens that were reed from the dataset along with the cause for removal is documented in the material propedata report, NCAMP Test Report CAM-RP-2015-038 Rev N/C.

Outliers for which no causes could be identified are